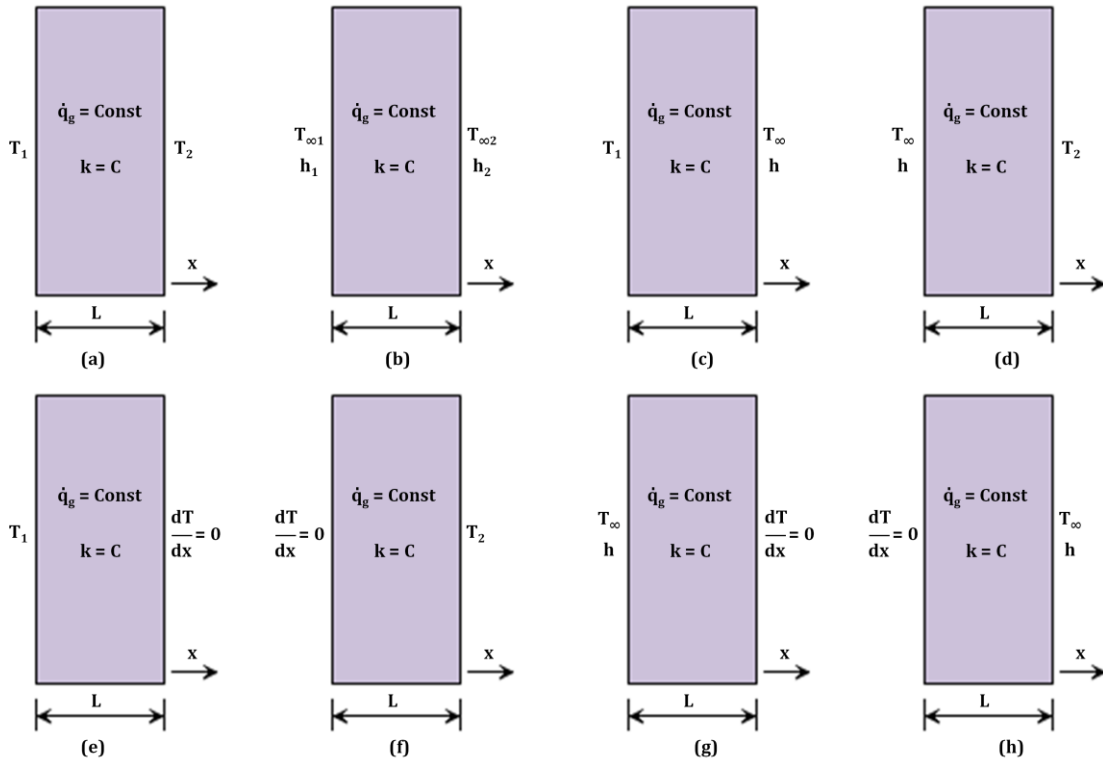
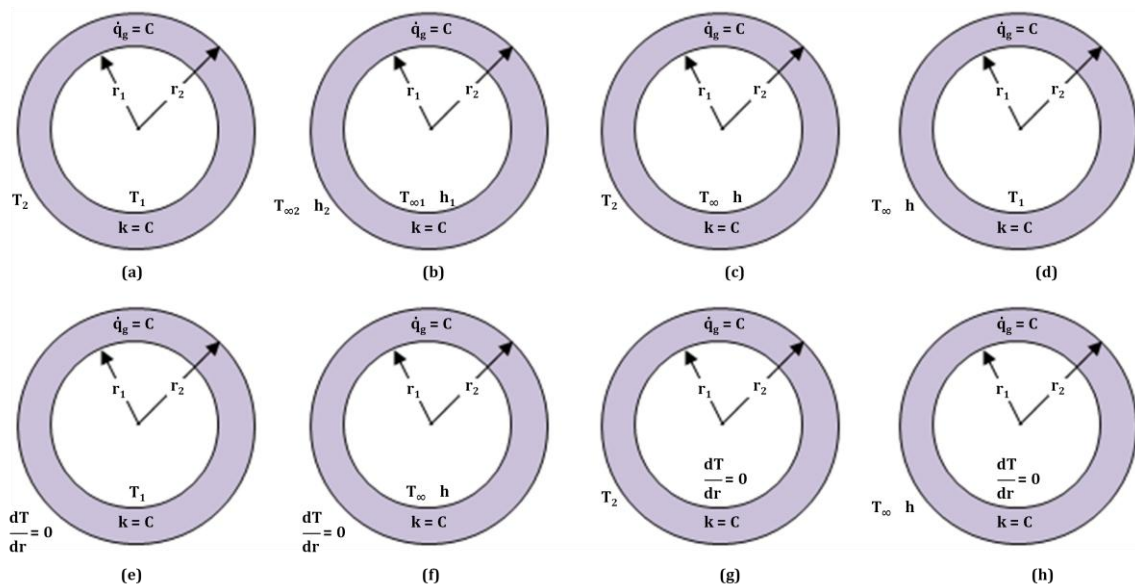




1. Consider a large 3 cm thick stainless steel plate ($k = 15.1 \text{ W/m} \cdot ^\circ\text{C}$) in which heat is generated uniformly at a rate of $5 * 10^5 \text{ W/m}^3$. Both sides of the plate are exposed to an environment at 30°C with a heat transfer coefficient of $60 \text{ W/m}^2 \cdot ^\circ\text{C}$. Obtain a relation for the variation of temperature in the wall by solving the differential equation, and determine the location and value of maximum temperature.
2. Consider a large 5 cm thick brass plate ($k = 111 \text{ W/m} \cdot ^\circ\text{C}$) in which heat is generated uniformly at a rate of $2 * 10^5 \text{ W/m}^3$. One side of the plate is insulated while the other side is exposed to an environment at 25°C with a heat transfer coefficient of $44 \text{ W/m}^2 \cdot ^\circ\text{C}$. Obtain a relation for the variation of temperature in the wall by solving the differential equation, and determine the location and value of maximum temperature.
3. A semiconductor material of thermal conductivity $k = 2 \text{ W/m} \cdot ^\circ\text{C}$ and electrical resistivity $\rho_e = 2 * 10^{-5} \Omega \cdot \text{m}$ is used to fabricate a cylindrical rod 10 mm in diameter and 40 mm long. The longitudinal surface of the rod is well insulated, while the ends are maintained at temperatures of 0 and 100°C . If the rod carries a current of 10 A, what is its midpoint temperature?
4. Consider a large plane wall of thickness $L = 0.05 \text{ m}$. The wall surface at $x = 0$ is insulated, while the surface at $x = L$ is maintained at a temperature of 30°C . The thermal conductivity of the wall is $k = 30 \text{ W/m} \cdot ^\circ\text{C}$, and heat is generated in the wall at a rate of $\dot{q} = Bx^2 \text{ W/m}^3$ where $B = 9.6 * 10^7 \text{ W/m}^5$. Assuming steady one-dimensional heat transfer. Obtain a relation for the variation of temperature in the wall by solving the differential equation and determine the temperature of the insulated surface of the wall.
5. Consider a large 5 cm thick brass plate ($k = 111 \text{ W/m} \cdot ^\circ\text{C}$) in which heat is generated uniformly at a rate of $2 * 10^5 \text{ W/m}^3$. One side of the plate is exposed to an environment at 40°C with a heat transfer coefficient of 52 W/m^2 while, the other side is exposed to an environment at 25°C with a heat transfer coefficient of $44 \text{ W/m}^2 \cdot ^\circ\text{C}$.
 - a) Drive the relation for the variation of temperature in the wall by solving the differential equation,
 - b) Determine the location and value of maximum temperature,
 - c) Determine both surfaces temperatures.
6. In a nuclear reactor, 1 cm diameter cylindrical uranium rods cooled by water from outside serve as the fuel. Heat is generated uniformly in the rods ($k = 29.5 \text{ W/m} \cdot ^\circ\text{C}$) at a rate of $7 * 10^7 \text{ W/m}^3$. If the outer surface temperature of rods is 175°C , determine the temperature at their center.
7. A copper cable ($k = 400 \text{ W/m} \cdot ^\circ\text{C}$) of 30 mm diameter has an electrical resistance of $5 * 10^{-3} \Omega/\text{m}$ and is used to carry an electrical current of 250 A. The cable is exposed to ambient air at 20°C , and the associated convection coefficient is $25 \text{ W/m}^2 \cdot ^\circ\text{C}$. What is the centerline and surface temperature of the wire?
8. In a long cylindrical fuel element in a nuclear reactor; energy generation occurs uniformly in the thorium fuel rod, which is of diameter $D = 25 \text{ mm}$ and is wrapped in a thin aluminum cladding. It is proposed that, under steady state conditions, the system operates with a generation rate of $\dot{q} = 7 * 10^8 \text{ W/m}^3$ and cooling system characteristics of $T_\infty = 95^\circ\text{C}$ and $h = 7000 \text{ W/m}^2 \cdot ^\circ\text{C}$. The thermal conductivity and melting point temperature of the thorium fuel are $60 \text{ W/m} \cdot \text{K}$ and 2023 K respectively, while the melting point temperature of aluminum is 933 K . Is this proposal satisfactory?
9. A chemical reaction takes place in a packed bed between two coaxial cylinders with radii 1 cm and 3 cm. The inner is at 500°C and it is insulated. Assuming the reaction rate of $6 * 10^5 \text{ W/m}^3$ in the reactor volume, find out the temperature at the outer surface of the reactor. Take k (packed material) = $0.5 \text{ W/m} \cdot \text{K}$.
10. Drive the temperature distribution, $T(x)$, and heat flow rate, $q(x)$, for one-dimensional, plane wall with the following boundary conditions where the thermal conductivity, k , and internal volumetric heat generation \dot{q}_g are constants.



11. Drive the temperature distribution, $T(r)$, and heat flow rate, $q(r)$, for one-dimensional, hollow cylinder with the following boundary conditions where the thermal conductivity, k , and internal volumetric heat generation \dot{q}_g are constants



12. Drive the formulas of radial distributions of temperature, and heat rate for a solid wire carrying an electric current I and the electrical resistance of the wire is R . The external surface with the following boundary condition

